

VASP exercises II

Outline

- Fcc Si
 - lattice relaxation

Fcc Si

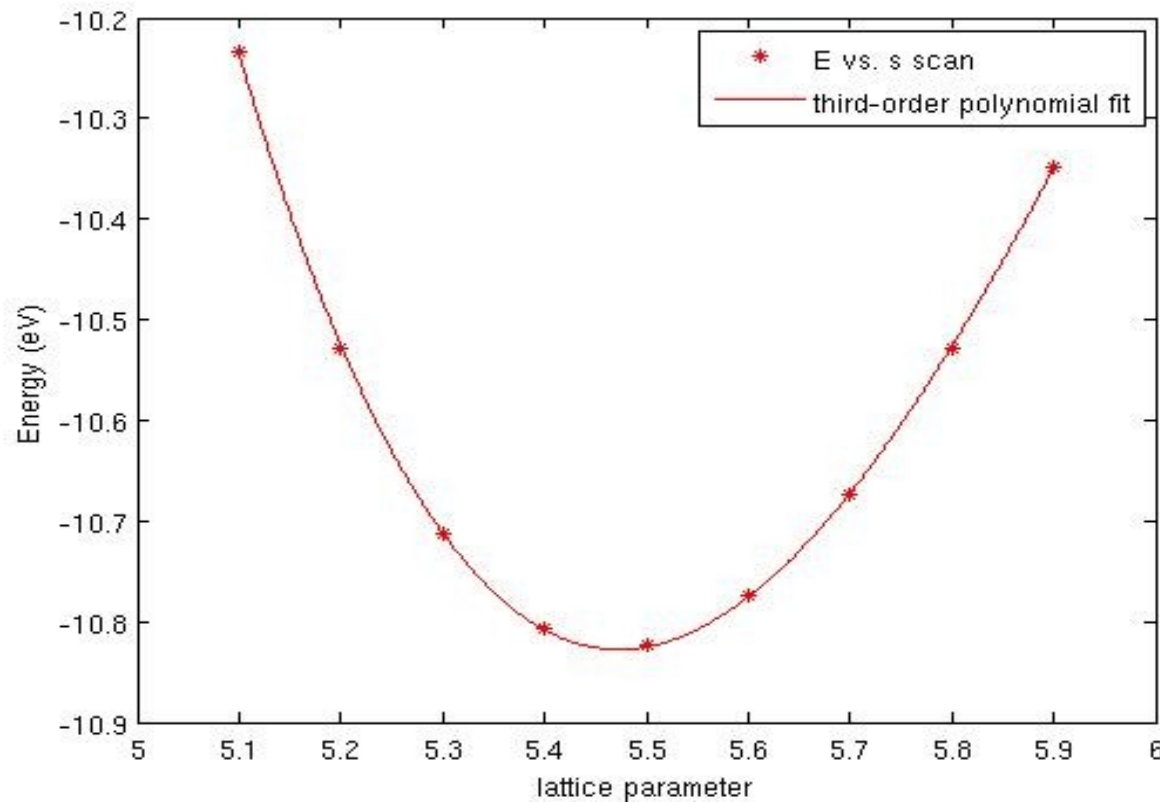
- search for the optimal volume (lattice parameter)
 - use of equation of state (EOS) for solids, which relates the energy of the system to the its volume
 - e.g. harmonic solid
 - or more sophisticated third-order Birch Murnaghan EOS

$$E = E_0 + \frac{1}{2}B_0 \frac{(V - V_0)^2}{V_0}.$$

$$E(V) = E_0 + \frac{9V_0B_0}{16} \left\{ \left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^3 B'_0 + \left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^2 \left[6 - 4 \left(\frac{V_0}{V} \right)^{\frac{2}{3}} \right] \right\}.$$

Fcc Si

- search for the minimum energy
- use of energy vs. lattice parameter scan to the its



- generally - the polynomial fit of E over a certain volume range
 - if no internal degrees of freedom present (e.g. the non-cubic cell, or more atoms in the primitive cell) – possible to use E vs. lattice parameter fit
 - if internal degrees present – the optimization of atomic positions or/and shape needed – controlled by the ISIF keyword (ISIF = 4)
- find the minimum => the optimal lattice parameter

Fcc Si

ISIF: - determines which degrees of freedom are allowed to change
=2 – (default) internal degrees of freedom (IDF) are relaxed
=3 – full relaxation (volume, cell shape, IDF)
=4 – IDF and cell shape is optimized

- search for the optimal lattice parameter

- use of equation of state (EOS) for solids, which relates the energy of the system to the its volume

- e.g. harmonic solid

$$E = E_0 + \frac{1}{2}B_0 \frac{(V - V_0)^2}{V_0}.$$

- or more sophisticated third-order Birch Murnaghan EOS

$$E(V) = E_0 + \frac{9V_0B_0}{16} \left\{ \left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^3 B'_0 + \left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^2 \left[6 - 4 \left(\frac{V_0}{V} \right)^{\frac{2}{3}} \right] \right\}.$$

- generally - the polynomial fit of E over a certain volume range
 - if no internal degrees of freedom present (e.g. the non-cubic cell, or more atom in the primitive cell) – possible to use E vs. lattice parameter fit
 - if internal degrees present – the optimization of atomic positions or/and shape needed – controlled by the ISIF keyword (ISIF = 4 or 2 for cubic cell)
- find the minimum => the optimal lattice parameter
- simpler “automatic” approach – full relaxation (internal degrees + volume) – ISIF = 3
 - but problematic due to basis set incompleteness – Pulay stress

Fcc Si – Pulay stress

$$\mathbf{b}_1 = 2\pi \frac{\mathbf{a}_2 \times \mathbf{a}_3}{\mathbf{a}_1 \cdot (\mathbf{a}_2 \times \mathbf{a}_3)}$$

$$|\mathbf{G} + \mathbf{k}| < G_{\text{cut}} \quad \text{with} \quad E_{\text{cut}} = \frac{\hbar^2}{2m} G_{\text{cut}}^2$$

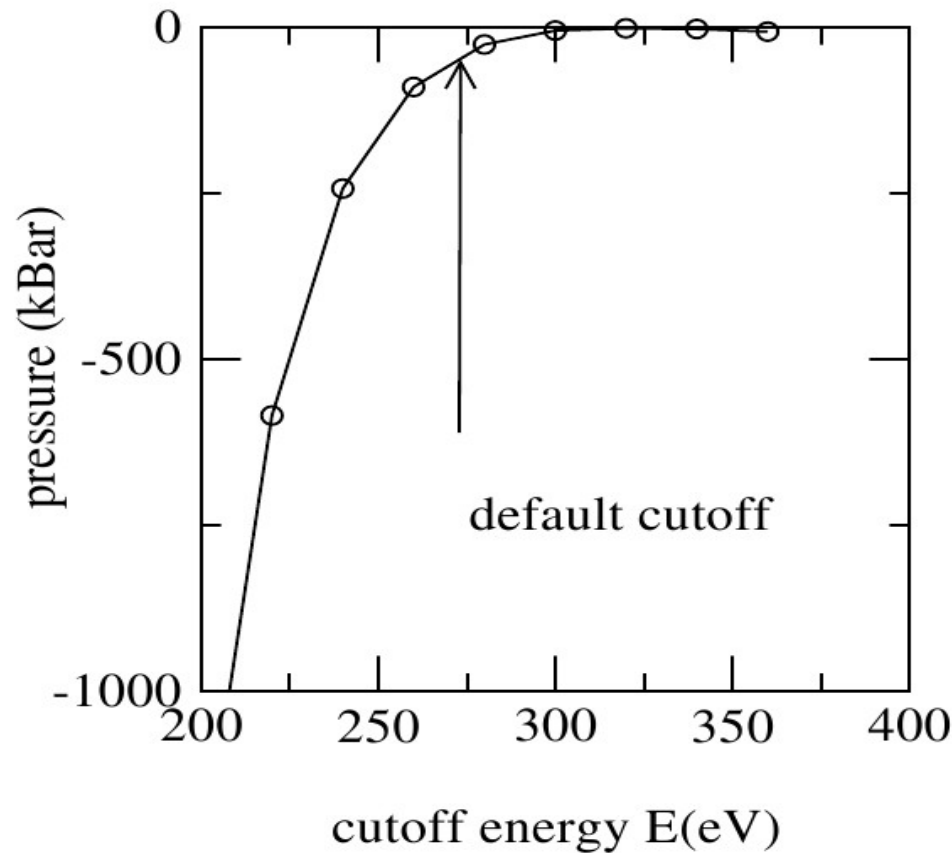
- the volume relaxation algorithm (ISIF = 3) works with the fixed basis set size
 - the same number of plane waves for larger volume leads effectively to smaller cutoff
 - => the energy is too high for larger volumes
 - => the equilibrium volume is thus too small
- the effect is due to basis set incompleteness – i.e. the due to Pulay stress (force)
 - increase of the cutoff by 30% (compared to default one) and rerun the optimization

$$\mathbf{G} = x_1^* \mathbf{b}_1 + x_2^* \mathbf{b}_2 + x_3^* \mathbf{b}_3$$

Fcc Si – Pulay stress

$$\mathbf{b}_1 = 2\pi \frac{\mathbf{a}_2 \times \mathbf{a}_3}{\mathbf{a}_1 \cdot (\mathbf{a}_2 \times \mathbf{a}_3)}$$

$$|\mathbf{G} + \mathbf{k}| < G_{\text{cut}} \quad \text{with} \quad E_{\text{cut}} = \frac{\hbar^2}{2m} G_{\text{cut}}^2$$



thm (ISIF = 3)

et size

$$\mathbf{G} = x_1 \cdot \mathbf{b}_1 + x_2 \cdot \mathbf{b}_2 + x_3 \cdot \mathbf{b}_3$$

aves for larger volume
utoff

larger volumes

thus too small

incompleteness –

- increase of the cutoff by 30% (compared to default one) and rerun the optimization

Fcc Si - VASP run

- `cd cviceni_2/ex_1`
- POTCAR for si at
`~grajciar/School/QCH../potpaw_PBE/Si`

- INCAR

```
SYSTEM = Si diamond      !title (optional)
ISMEAR = 0 ; SIGMA = 0.1
ENCUT = 240
```

- KPOINTS

```
Automatic mesh
0                !automatic generation ('zero')
Monkhorst Pack  !method of automatic generation
11 11 11        !num. of subdivisions along reciprocal vectors
0 0 0           !shift of the k-point mesh
```

- POSCAR

```
fcc Si
3.9
0.5 0.5 0.0
0.0 0.5 0.5
0.5 0.0 0.5
Si
1
Cartesian
0 0 0
```


Fcc Si - VASP run

- we shall use simple bash script to obtain the E vs. lattice parameter scan – scan.sh

- generates geom_scan.dat file

3.5	-.44256712E+01
3.6	-.46614699E+01
3.7	-.47979864E+01
3.8	-.48645041E+01
3.9	-.48773847E+01
4.0	-.48487437E+01
4.1	-.47852634E+01
4.2	-.46936947E+01
4.3	-.45831167E+01

- find the optimal lattice parameter by fitting to polynomial in MATLAB
- 3,874 Å – optimal value

```
#!/bin/bash
rm WAVECAR CONTCAR
for i in 3.5 3.6 3.7 3.8 3.9 4.0 4.1 4.2 4.3
do
  #for i in 4.2 4.3
  rm CONTCAR
  cat > POSCAR <<EOF
fcc Si
  $i
    0.5  0.5  0.0
    0.0  0.5  0.5
    0.5  0.0  0.5
  Si
  1
  Cartesian
    0  0  0
  EOF
  echo "parameter = $i"
  VASP mq 8 1.3G
  while [ ! -s CONTCAR ];do
    sleep 5
  done

  E=`tail -1 OSZICAR|awk '{print $3}'`
  echo $i $E >> geom_scan.dat
done
```

Fcc Si - full relaxation

- `cd ../ex_2`

- POTCAR, KPOINTS and POSCAR from previous run

- INCAR

```
SYSTEM = Si diamond           !title (optional)
ISMEAR = 0 ; SIGMA = 0.1
ENCUT = 240
IBRION = 2; ISIF = 3; NSW = 15
EDIFF = 0.1E-04
EDIFFG = -0.01                !conv. criteria for ionic steps
```

EDIFFG: determines the convergence criteria for the ionic relaxation
=real number (positive if the change in the energies is smaller than EDIFFG
negative if the change of all forces is less then |EDIFFG|
Default = EDIFF*10

-

Fcc Si - full relaxation

- cd ../ex_2

- POTCAR, KPOINTS and POSCAR from previous run

- INCAR

```
SYSTEM = Si diamond           !title (optional)
ISMEAR = 0 ; SIGMA = 0.1
ENCUT = 240
IBRION = 2; ISIF = 3; NSW = 15
EDIFF = 0.1E-04
EDIFFG = -0.01                !conv. criteria for ionic steps
```

- CONTCAR

- optimal lattice from full relaxation is
3.867 Å

- smaller than form E vs. lattice parameter fit
3.874 Å – due to Pulay stress

EDIFFG: determines the convergence criteria for the ionic relaxation
=real number (positive if the change in the energies is smaller than EDIFFG
negative if the change of all forces is less then |EDIFFG|
Default = EDIFF*10

```
fcc Si
3.9000000000000000
0.4957651233838283 0.4957651233838283 0.0000000000000000
0.0000000000000000 0.4957651233838283 0.4957651233838283
0.4957651233838283 0.0000000000000000 0.4957651233838283
Si
1
Direct
0.0000000000000000 0.0000000000000000 0.0000000000000000

0.000000000E+00 0.000000000E+00 0.000000000E+00
```

Outline

- Fcc Si
 - lattice relaxation
 - k-points study

Fcc Si - k-points study

Automatic mesh

0

Monkhorst Pack

11 11 11

0 0 0

!automatic generation ('zero')

!method of automatic generation

!num. of subdivisions along reciprocal vectors

!shift of the k-point mesh

- what k-point mesh size to use?
- mind that number of k-points does not have to increase with mesh-size
 - e. g. for the FCC the even grids not centered at the Gamma(0,0,0) point are larger (e. g. 8x8x8=>60 k-points) than odd grids (9x9x9=>35 k-points)
- the grids centered at Gamma point (line 3 starting with 'G') might behave differently than e. g. Monkhorst Pack grid (line 3 starting with 'M') shifted away from Gamma point (see above)
- the actual k-points generated by automatic procedure are stored in IBZKPT file – this should be then directly related to the k-point sampling precision
- General recommendation:
 - use even meshes up to ~8 (8x8x8), use the odd meshes from there up (e. g. 11x11x11)
 - check the IBZKPT file to see how many k-points have been actually generated
 - use 'G' grid for hexagonal lattices – 'M' grids effectively lowers the cell symmetry leading to slower convergence

Fcc Si - k-points study

- `cd ../ex_3/`
- copy POSCAR, INCAR and POTCAR from `ex_1`
- use `scan.sh` script to generate k-point scan
- run by `./scan.sh`
- various files generated
- `scan.dat` – mesh size vs. energy

```
1 0.64239277E+01
2 -.42083843E+01
3 -.47424589E+01
4 -.45562350E+01
5 -.45498122E+01
6 -.45747892E+01
7 -.45680113E+01
8 -.45738961E+01
9 -.45954740E+01
```

```
#!/bin/bash
for i in 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
do
if [ -a OUTCAR ]
then
    rm OUTCAR
fi
touch OUTCAR
cat > KPOINTS <<EOF
K - points
0
Monkhorst Pack
$i $i $i
0 0 0
EOF
echo "parameter = $i"
VASP mq 8 1.3G
while [ "General" != "$(grep 'General timing' OUTCAR|awk '{print $1}')" ];do
sleep 5
done

E=`tail -1 OSZICAR|awk '{print $3}`
timing=`grep 'User time' OUTCAR|awk '{print $4}`
kpoints=`head -2 IBZKPT|tail -1`
echo $i $E >> scan.dat
echo $kpoints $E >> kpoints.dat
cp OUTCAR "OUTCAR_"$i
echo $i $timing >> timing.dat
echo $kpoints $timing >> kpoints_timing.dat
echo $i $kpoints >> kpoints_mesh.dat
done
```

Fcc Si - k-points study

- `cd ../ex_3/`
- copy POSCAR, INCAR and POTCAR from ex_1
- use scan.sh script to generate k-point scan
- run by `./scan.sh`
- various files generated
- `kpoints_mesh.dat` – mesh size vs. actual number of k-points

```
1 1
2 2
3 4
4 10
5 10
6 28
7 20
8 60
9 35
```

```
#!/bin/bash
for i in 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
do
if [ -a OUTCAR ]
then
    rm OUTCAR
fi
touch OUTCAR
cat > KPOINTS <<EOF
K - points
0
Monkhorst Pack
$i $i $i
0 0 0
EOF
echo "parameter = $i"
VASP mq 8 1.3G
while [ "General" != "$(grep 'General timing' OUTCAR|awk '{print $1}')" ];do
sleep 5
done

E=`tail -1 OSZICAR|awk '{print $3}`
timing=`grep 'User time' OUTCAR|awk '{print $4}`
kpoints=`head -2 IBZKPT|tail -1`
echo $i $E >> scan.dat
echo $kpoints $E >> kpoints.dat
cp OUTCAR "OUTCAR_"$i
echo $i $timing >> timing.dat
echo $kpoints $timing >> kpoints_timing.dat
echo $i $kpoints >> kpoints_mesh.dat
done
```

Fcc Si - k-points study

- `cd ../ex_3/`
- copy POSCAR, INCAR and POTCAR from `ex_1`
- use `scan.sh` script to generate k-point scan
- run by `./scan.sh`
- various files generated
- `kpoints_timing.dat` – actual number of k-points vs. time

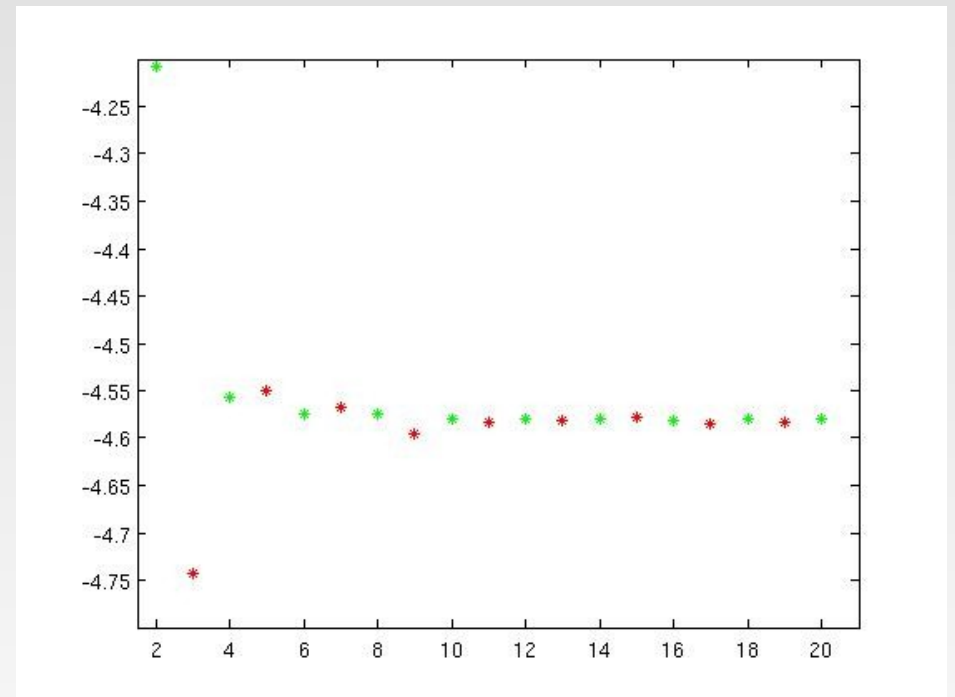
```
1 0.380
2 0.350
4 0.300
10 0.460
10 0.470
28 0.740
20 0.620
60 1.380
35 0.850
```

```
#!/bin/bash
for i in 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
do
if [ -a OUTCAR ]
then
    rm OUTCAR
fi
touch OUTCAR
cat > KPOINTS <<EOF
K - points
0
Monkhorst Pack
$i $i $i
0 0 0
EOF
echo "parameter = $i"
VASP mq 8 1.3G
while [ "General" != "$(grep 'General timing' OUTCAR|awk '{print $1}')" ];do
sleep 5
done

E=`tail -1 OSZICAR|awk '{print $3}`
timing=`grep 'User time' OUTCAR|awk '{print $4}`
kpoints=`head -2 IBZKPT|tail -1`
echo $i $E >> scan.dat
echo $kpoints $E >> kpoints.dat
cp OUTCAR "OUTCAR_"$i
echo $i $timing >> timing.dat
echo $kpoints $timing >> kpoints_timing.dat
echo $i $kpoints >> kpoints_mesh.dat
done
```

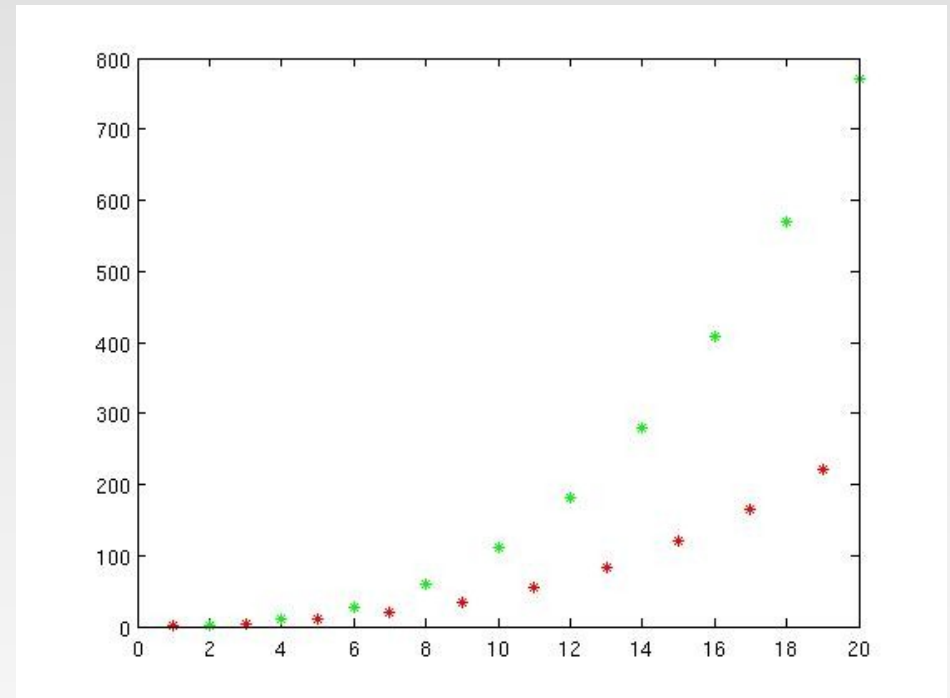

Fcc Si - k-points study

- load and visualize
 - the energy is converged for mesh size ~10 and more



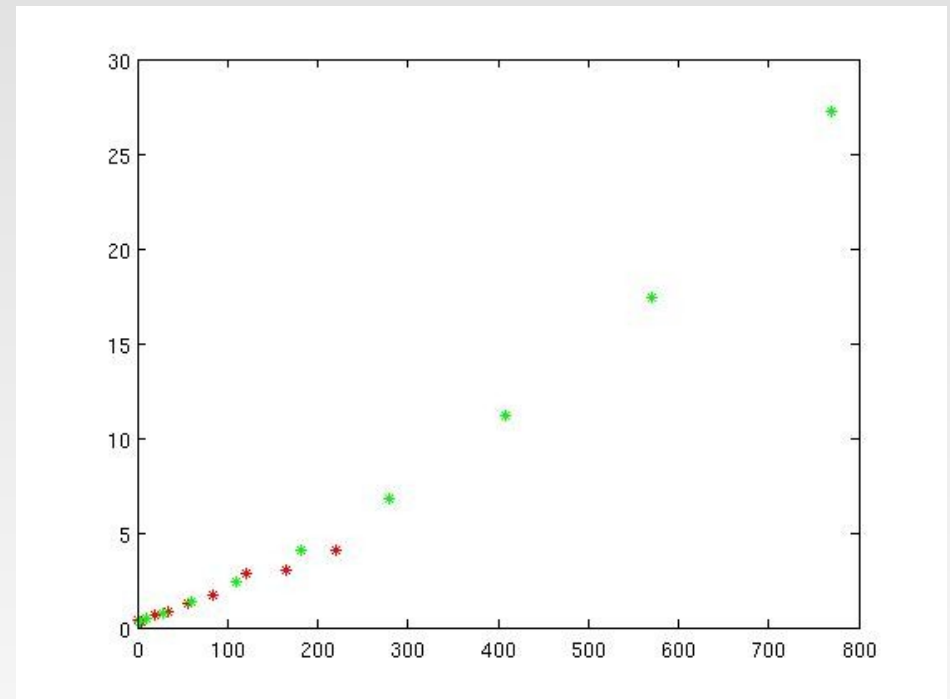
Fcc Si - k-points study

- load and visualize
 - the even k-point meshes generate in this case more k-points than comparable odd meshes
 - e. g. the 8x8x8 mesh contains the same number of k-points as the 11x11x11 odd mesh => always check the IBZKPT file to see the actual k-points number



Fcc Si - k-points study

- load and visualize
 - the linear dependence until about 200 k-points observed
 - slightly different behavior of odd and even grids



Outline

- Fcc Si
 - lattice relaxation
 - k-points study
- Diamond Si
 - DOS and band-structure calculation – insulator/semiconductor/metal

Density of states - DOS

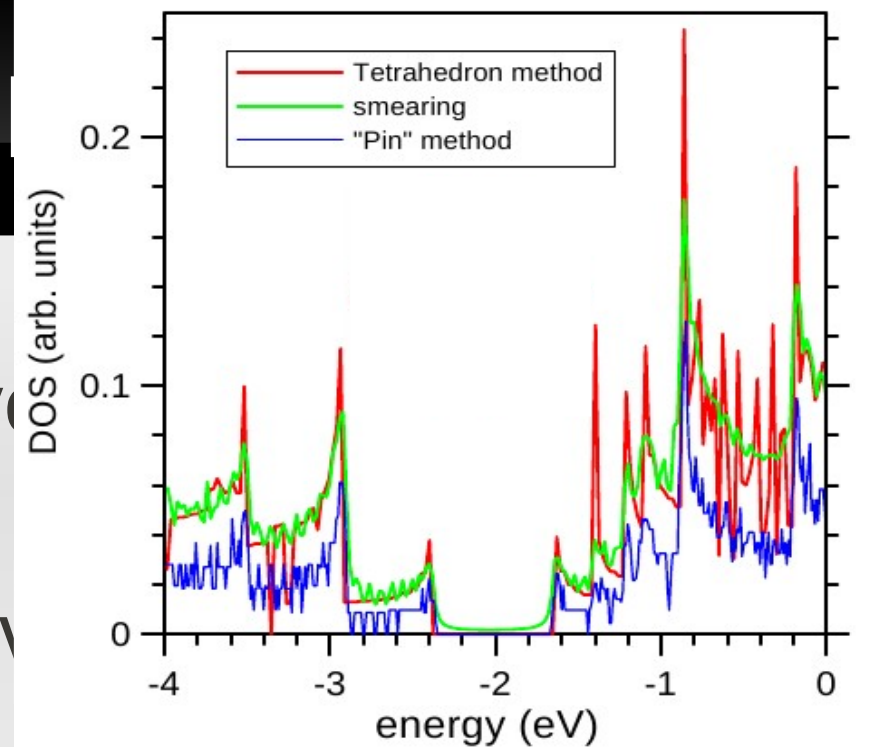
$$g(E) = \frac{1}{dE} \sum_E^{E+dE} 1$$

- the number of energy levels between E and $E + dE$ divided by the dE
- in periodic system sum over all possible k -point values

$$g(E) = \sum_k \delta(E - E(k))$$

Density of states -

- the number of energy levels in dE divided by the dE
- in periodic system sum over all k values
- in practice finite k -point mesh and dE set used
 - DOS vs. E plot is “spiky”
 - smearing of the spikes into smooth functions like gaussian (see smearing methods)
 - tetrahedron method (ISMEAR = -5) – interpolation between k -points
 - finer k -point grid needed



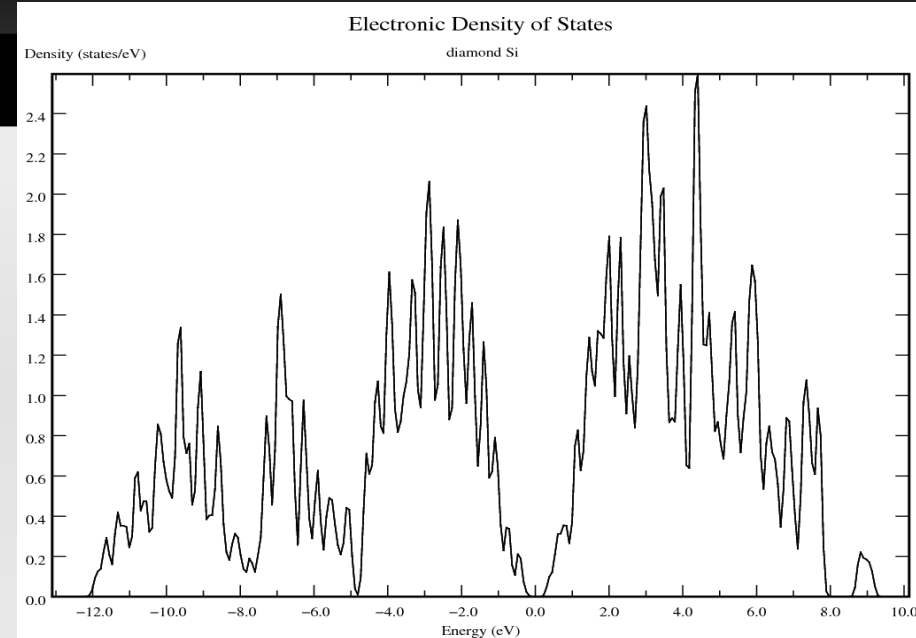
Diamond Si

- `cd cviceni_2/si_diamond/ex_1`
- POTCAR, INCAR and KPOINTS from `si_fcc/ex_1`
- POSCAR
- run VASP

```
diamond Si
5.5
0.0 0.5 0.5
0.5 0.0 0.5
0.5 0.5 0.0
Si
2
Direct
-0.125 -0.125 -0.125
0.125 0.125 0.125
```

Diamond Si - DOS

- DOS – directly from the last run
 - provided in DOSCAR file
 - use the visualization tool (p4vasp)
 - not accurate enough!
 - finer k-point mesh size needed => time consuming
 - two step calculation:
 - 1. self-consistent calculation with smaller number of k-points (already done)
 - 2a. increase of the number of k-points
 - 2b. while charge density converges fast with the number of k-points => non-self consistent calculation possible using the charge density from previous self-consistent run. The charge density is fixed. The k-points are treated independently.
 - 2c. controlled by ICHARG keyword (ICHARG = 11)



Diamond Si - DOS

ICHARG: determines how to construct initial charge density
0=calculate from initial wave-function (default if WAVECAR present)
1=read the density from CHGCAR
2=superposition of atomic densities (default if no WAVECAR present)
11=non-selfconsistent calculation – read in CHGCAR and do not update

- DOS – directly from the last run
 - provided in DOSCAR file
 - use the visualization tool (p4vasp)
 - not accurate enough!
 - finer k-point mesh size needed => time consuming
 - two step calculation:
 - 1. self-consistent calculation with smaller number of k-points (already done)
 - 2a. increase of the number of k-points
 - 2b. while charge density converges fast with the number of k-points => non-self consistent calculation possible using the charge density from previous self-consistent run. The charge density is fixed. The k-points are treated independently.
 - 2c. controlled by ICHARG keyword (ICHARG = 11)

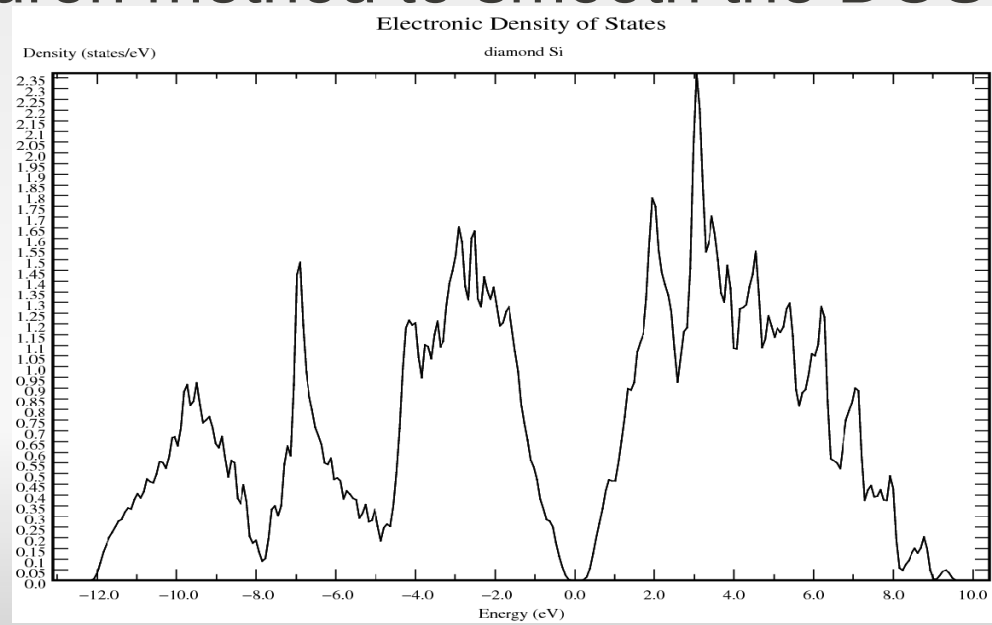
Diamond Si - DOS

- `cd cviceni_2/si_diamond/ex_2`
- POTCAR, POSCAR from `si_diamond/ex_1`

- INCAR

```
SYSTEM = Si diamond      !title (optional)
ISMEAR = -5              !linear tetrahedron method
SIGMA = 0.1
ENCUT = 240
ICHARG = 11              !read charge file and do not update
```

- besides finer k-point mesh also usage of linear tetrahedron method to smooth the DOS



Diamond Si - DOS

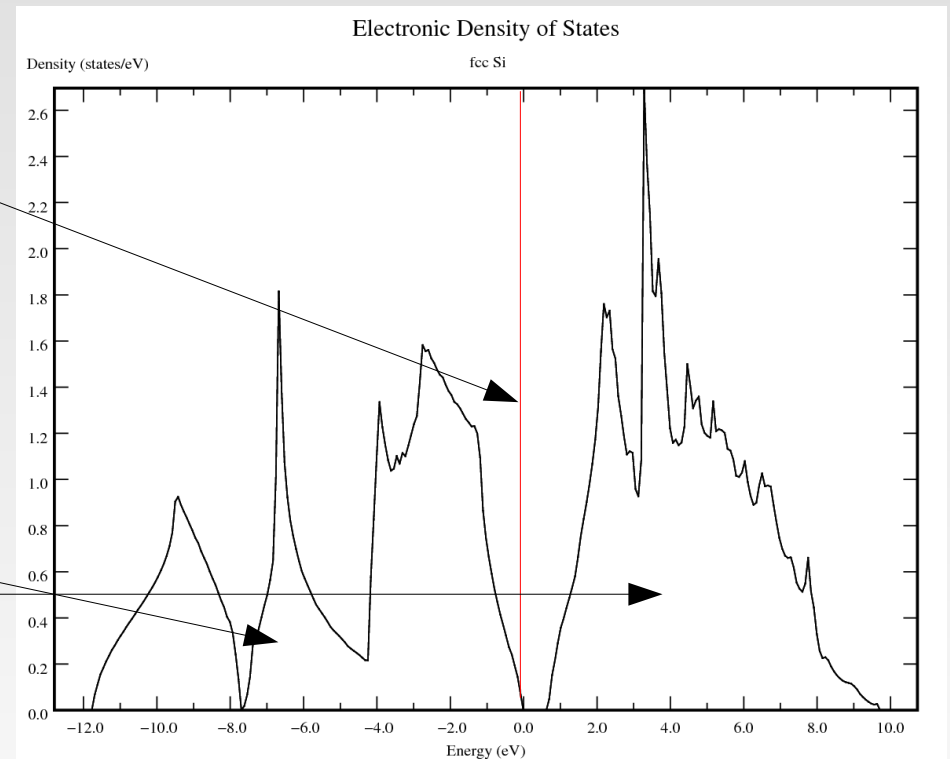
- `cd cviceni_2/si_diamond/ex_2`
- POTCAR, POSCAR from `si_diamond/ex_1`
- INCAR

SYSTEM = Si diamond	!title (optional)
ISMEAR = -5	!linear tetrahedron method
SIGMA = 0.1	
ENCUT = 240	
ICHARG = 11	!read charge file and do not update
- besides finer k-point mesh also usage of linear tetrahedron method to smooth the DOS
- KPOINTS

Automatic mesh	
0	!automatic generation ('zero')
Monkhorst Pack	!method of automatic generation
21 21 21	!num. of subdivisions along reciprocal vectors
0 0 0	!shift of the k-point mesh
- run VASP

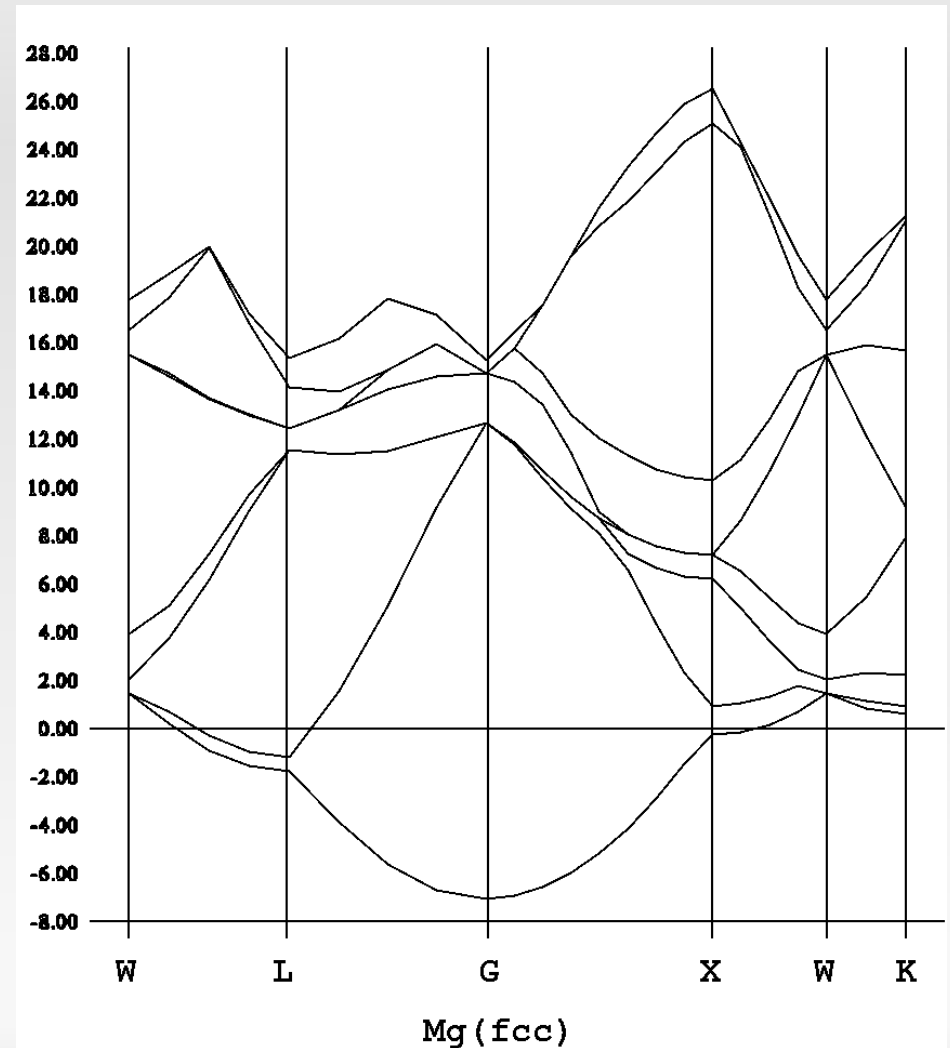
Diamond Si - DOS

- visualize with p4vasp
- smooth DOS observed
- a small gap (~ 0.6 eV) present on the Fermi level – semiconductor
- experimental band gap ~ 1.12
- valence bands
- conduction bands



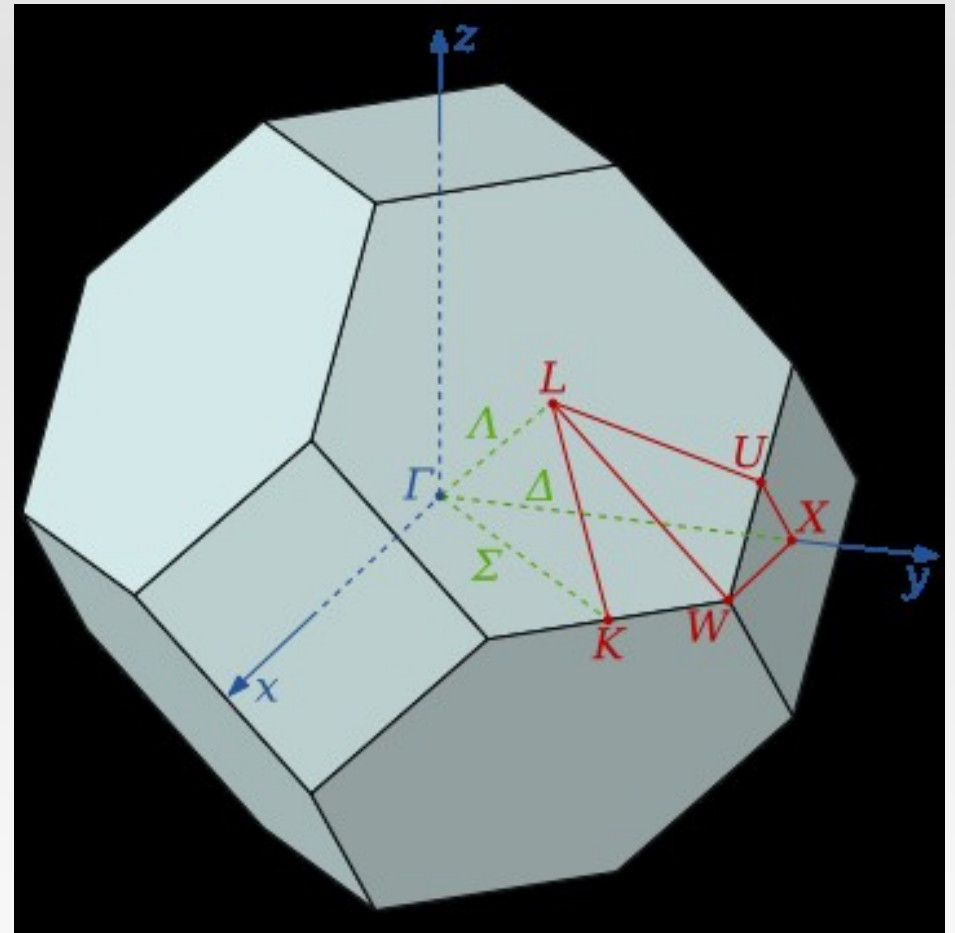
Diamond Si – Band structure

- Band structure
 - energy vs. k-point plot
 - 3D data (k is a vector) – need for a simplification



Diamond Si – Band structure

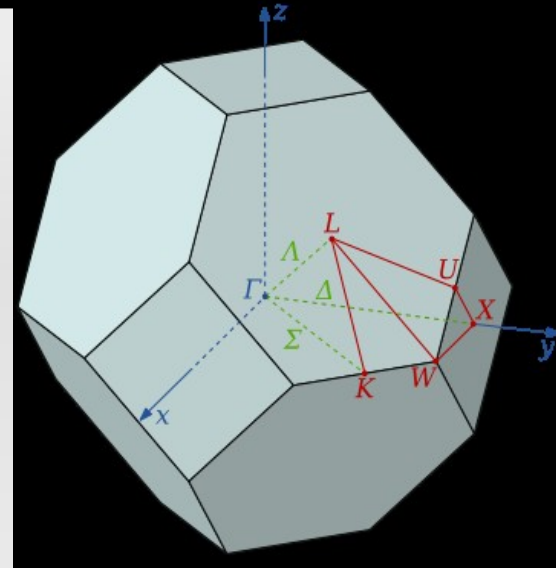
- Band structure
 - energy vs. k-point plot
 - 3D data (k is a vector) – need for a simplification
 - the plot along specific lines within Brillouin zone(BZ)
 - Γ – gamma point – center of BZ
 - X – center of face
 - L – center of hexagonal face ...
 - energies(eigenvalues) for various k-points stored in EIGENVAL file



Diamond Si – Band structure

- `cd cviceni_2/si_diamond/ex_3`
- POTCAR, POSCAR from `si_diamond/ex_1`
- INCAR

```
SYSTEM = fcc Si
ICHARG = 11
ENCUT = 240
ISMEAR = 0; SIGMA=0.1
```



- use `ICHARG = 11` – the k-point mesh is not regular – need of self-consistent density with regular mesh beforehand
- KPOINTS
 - 3rd line with tag 'line'
- Run VASP

```
k-points for bandstructure L-G-X-U K-G
10                               !number of points between k-point couples
line
reciprocal
0.5 0.5 0.5 1                   !L
0.0 0.0 0.0 1                   !G

0.0 0.0 0.0 1                   !G
0.0 0.5 0.5 1                   !X

0.0 0.5 0.5 1                   !X
0.25 0.625 0.625 1              !U

0.375 0.75 0.375 1              !K
0.0 0.0 0.0 1                   !G
```

Diamond Si – Band structure

Energies(eigenvalues) for various k-points
are stored in EIGENVAL file

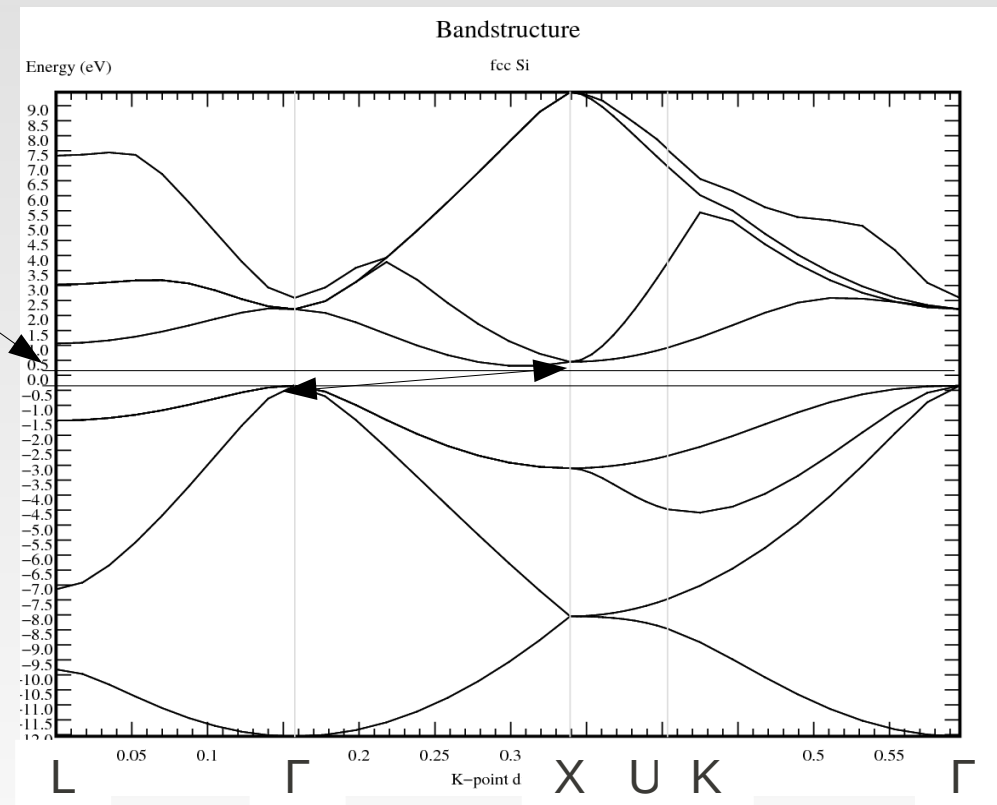
- Band structure
 - energy vs. k-point plot
 - forbidden band
 - indirect gap
 - conduction and valence s(p) bands
 - the plot along specific lines within Brillouin zone(BZ)

Γ – gamma point – center of BZ

X – center of face

L – center of hexagonal face

etc.

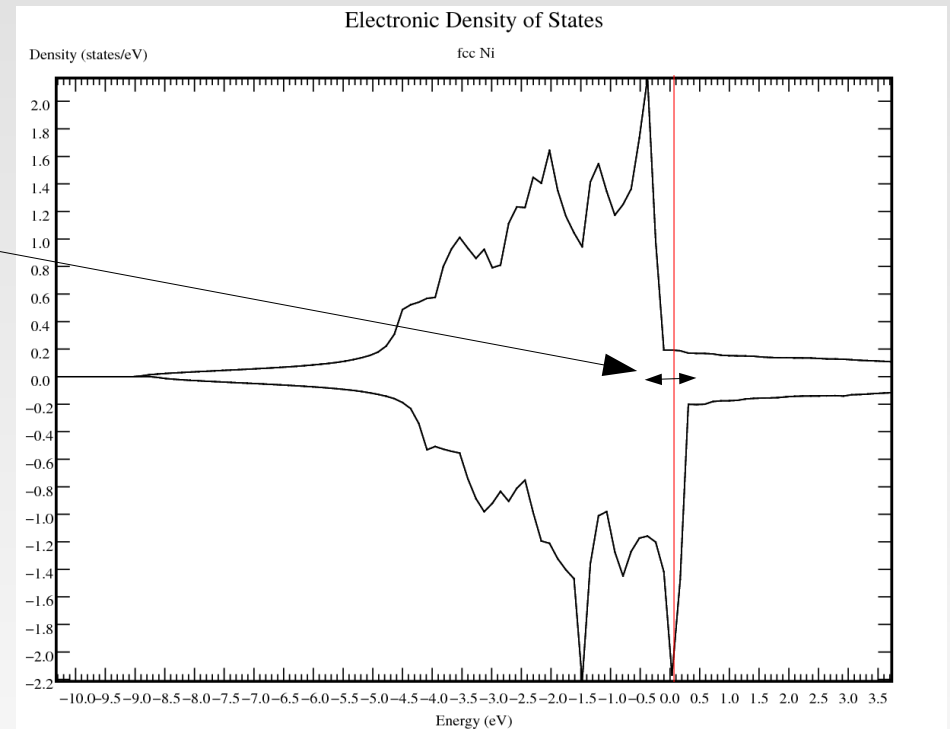


Outline

- Lattice parameter
 - fcc Si
- DOS and band-structure calculation – insulator/semiconductor/metal
 - Diamond Si
 - fcc Ni - metal

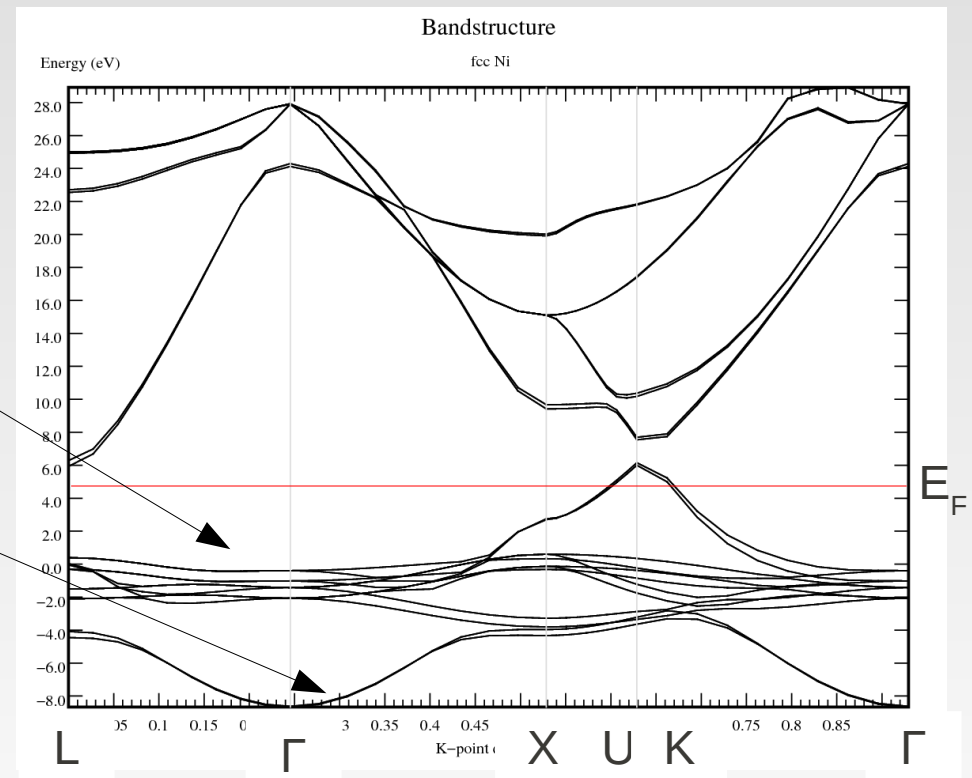
fcc Ni - DOS

- calculate like in diamond Si case (optional)
- DOS for the spin up and spin down
- exchange splitting on the Fermi level
- no band gap present on the Fermi level – metal



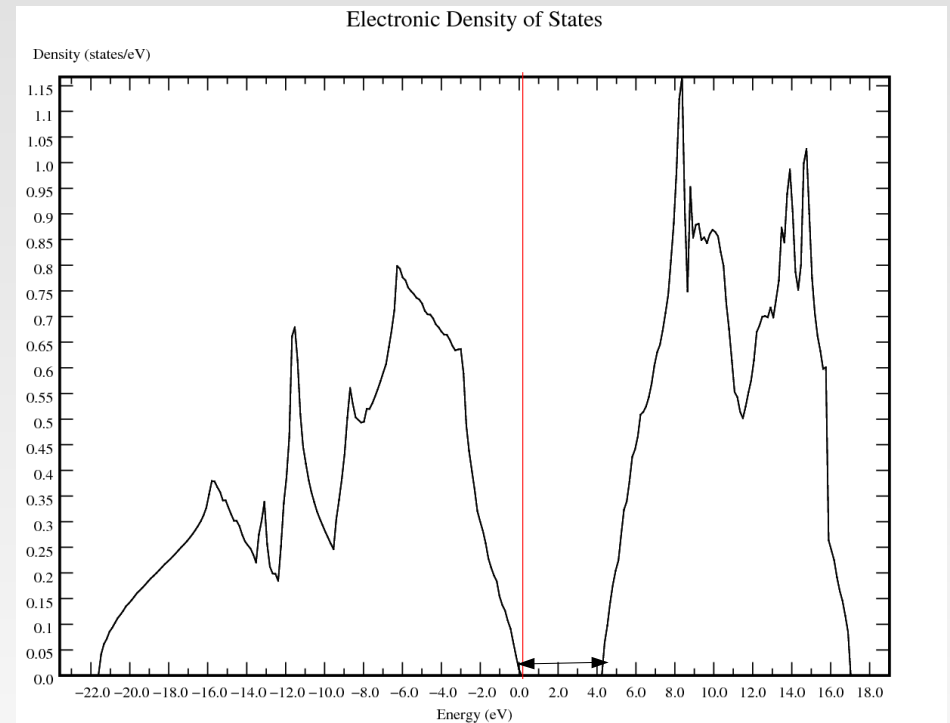
Fcc Ni – Band structure

- Band structure
 - energy vs. k-point plot
 - no gap at Fermi level
 - s(p) and d bands
 - Fermi level – 4,67 eV



Diamond C – insulator - DOS

- calculate like in diamond Si case (optional)
- large band gap (~ 4 eV) – exp. ~ 5.5 eV



Diamond Si – Band structure

Energies(eigenvalues) for various k-points
are stored in EIGENVAL file

- Band structure
 - energy vs. k-point plot
 - large band gap
 - s(p) bands

